## MEAN, MEDIAN AND MODE

1. At a pet store, a survey was taken asking how many pets each person had. The results were: $2,5,3,1,0,4,2,7,0,2,7,3,2,4,3$. Find the following:
a) Mean
b) Median
c) Mode

2. Forty students took a math test marked out of ten points. Their results are as follows:
$9,10,7,8,9,6,5,9,4,7,1,7,2,7,8,5,4,3,10,7,3,7,8,6,9,7,4,2,3,9,4,3$, $7,5,5,2,7,9,7,1$
a) Prepare a frequency table of the scores
b) Using the frequency table, calculate the mean, median, mode, and range.
c) Draw a bar chart to represent the data.
3. The table shows data of heights of people in a sample of people in $3^{\text {rd }}$ ESO:

| Height $(\mathrm{cm})$ | Frequency |
| :---: | :---: |
| $[130,140)$ | 7 |
| $[140,150)$ | 12 |
| $[150,160)$ | 16 |
| $[160,170)$ | 5 |
| $[170,180)$ | 2 |

a) Find the range of heights.
b) Find the median class.
c) What is the modal class?
d) Find an estimate of the mean height.
e) Draw a histogram to represent the data.
4. The following are heights of small Christmas trees in cm . The heights are between 21 cm and 66 cm
$65,32,54,56,34,43,21,51,50,61,59,45,48,39,41,31,36,65,66,44,45,40$, $30,50,57,32,61,48,55,45,35,30,32,45,39,32,49,47,55,34,53,43,59,41$
a) Draw a stem and leaf diagram for the data (use intervals of 10 cm ).
b) Find the mean height.
c) Find the range of the heights
d) Draw a histogram to represent the data.


## SOLUTION

1. At a pet store, a survey was taken asking how many pets each person had. The results were: $2,5,3,1,0,4,2,7,0,2,7,3,2,4,3$.
First, we order the data: $0,0,1,2,2,2,2,3,3,3,4,4,5,7,7$
Mean: $\bar{x}=\frac{1+2+2+2+2+3+3+3+4+4+5+7+7}{15}=3$ pets
Mode (the most common value in the data set): 2 pets
Median (value of "middle" data item): 2.5
2. Frequency table:

| Marks <br> $x$ | Frequency <br> $f$ | Cumulative <br> Frequency (F) | $x \cdot f$ |
| :---: | :---: | :---: | :---: |
| 1 | 2 | 2 | 2 |
| 2 | 3 | 5 | 6 |
| 3 | 4 | 9 | 12 |
| 4 | 4 | 13 | 16 |
| 5 | 4 | 17 | 20 |
| 6 | 2 | 19 | 12 |
| 7 | 10 | 29 | 70 |
| 8 | 3 | 32 | 24 |
| 9 | 6 | 38 | 54 |
| 10 | 2 | 40 | 20 |
| Total | 40 |  | 236 |

Mean: $\bar{x}=\frac{236}{40}=5.9$ points
Range: 10-1 = 9 points
Mode: 7 points
Median: $40: 2=20 \rightarrow \mathrm{~F}>20 \rightarrow 29 \rightarrow 7$ points is the median Bar chart:

3. Range of heights: $180-130=50 \mathrm{~cm}$

| Height (cm) | Mid-point $(x)$ | Frequency $(f)$ | Cumulative f.(F) | $x \cdot f$ |
| :---: | :---: | :---: | :---: | :---: |
| $[130,140)$ | 135 | 7 | 7 | 945 |
| $[140,150)$ | 145 | 12 | 19 | 1740 |
| $[150,160)$ | 155 | 16 | 35 | 2480 |
| $[160,170)$ | 165 | 5 | 40 | 825 |
| $[170,180)$ | 175 | 2 | 42 | 350 |
|  | Total | 42 |  | 6340 |

Median: $42: 2=21 \rightarrow 35>21 \rightarrow[150,160)$ is the median class
Modal: $[150,160)$ is the modal class
Mean height. $\bar{x}=\frac{6340}{42}=150.95$
Draw a histogram to represent the data:

4. The following are heights of small Christmas trees in cm . The heights are between 21 cm and 66 cm
$65,32,54,56,34,43,21,51,50,61,59,45,48,39,41,31,36,65,66,44,45,40$, $30,50,57,32,61,48,55,45,35,30,32,45,39,32,49,47,55,34,53,43,59,41$

Stem and leaf diagram for the data (use intervals of 10 cm ):

| Height $(\mathrm{cm})$ | Mid-point $(x)$ | Frequency $(f)$ | $x \cdot f$ |
| :---: | :---: | :---: | :---: |
| $[20,30)$ | 25 | 1 | 25 |
| $[30,40)$ | 35 | 13 | 455 |
| $[40,50)$ | 45 | 14 | 630 |
| $[50,60)$ | 55 | 11 | 605 |
| $[60,70)$ | 65 | 5 | 325 |
|  |  | 44 | 2040 |

Mean height: $\bar{x}=\frac{2040}{44}=46.36 \mathrm{~cm}$
Range of the heights: 66-21 $=45 \mathrm{~cm}$
Histogram:


