

EXAM 2_2 (Functions 2)

Name:.....

1. Solve algebraically and graphically the simultaneous equations (to graph the functions write their characteristics and **don't** use a table data):

$$y = \sqrt{2x + 1}$$

$$y = \frac{x}{2} + 1$$
(2 points)

- 2. The labels stuck on tins of tomatoes are rectangular which an area of 18 cm². What are the possible lengths of the base and height? Make a table with some of the possibilities and graph the function. Find the rule. What type of function is it?
- 3. Sketch the graph of the compound function (to graph the function write its characteristics and don't use a table data):

$$f(x) = \begin{cases} 2 - 2x & x < 0\\ 2 - x^2 & 0 \le x < 3\\ -3 & x \ge 3 \end{cases}$$
 (2 points)

- a) Domain and range
- b) Increasing and decreasing intervals
- c) Continuity
- 4. In the following equations, find x: (2 points)
 - a) $\log_3 9^x = 2$ b) $\log_5(x+2) = 3$

c)
$$3^{x^2-6} = \frac{1}{27}$$
 d) $\log_x 16 = -2$

5. Sketch the graph of the function $y = \left(\frac{1}{2}\right)^x$ What type of function is it? Write its characteristics.

Using the basic $y = \left(\frac{1}{2}\right)^x$, sketch the graph of $y = \left(\frac{1}{2}\right)^x - 2$ and $y = \left(\frac{1}{2}\right)^{x+3}$. Find their intersections with x-axis and y-axis, if possible, their domains, ranges and asymptotes. (2 points)



1.

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SOLUTION

$$\begin{array}{c} \gamma = \sqrt{2x+1} \\ \gamma = \frac{x}{2}+1 \end{array} \right\} \Rightarrow \sqrt{2x+1} = \frac{x}{2}+1 \Rightarrow 2\sqrt{2x+1} = x+2 \Rightarrow \left(2\sqrt{2x+1}\right)^2 = (x+2)^2$$

$$4(2x+1) = x^2 + 4x + 4 \Longrightarrow 8x + 4 = x^2 + 4x + 4 \Longrightarrow x^2 - 4x = 0 \Longrightarrow x = 0, x = 4$$

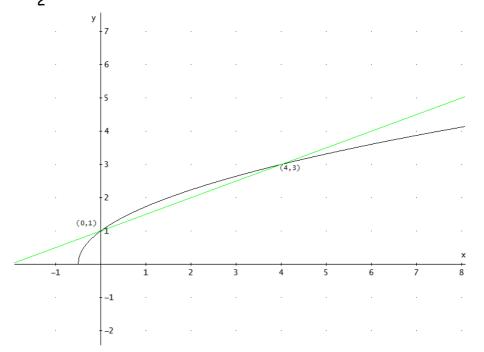
Checking:
$$\sqrt{2x+1} = \frac{x}{2} + 1 \Longrightarrow \begin{cases} \sqrt{2 \cdot 0} + 1 = 0 + 1 \Longrightarrow 1 = 1 \lor \\ \sqrt{2 \cdot 4} + 1 = 2 + 1 \Longrightarrow 3 = 3 \lor \end{cases}$$

Solution: they intercepts in (0,1) and (6,4)

Graphically: $y = \sqrt{2x+1}$ it is a radical function (semi-parabola) with domain:

$$2x+1 \ge 0 \Longrightarrow 2x \ge 1 \Longrightarrow x \ge \frac{1}{2} \to \text{Dom} = \left[\frac{1}{2}, +\infty\right]$$

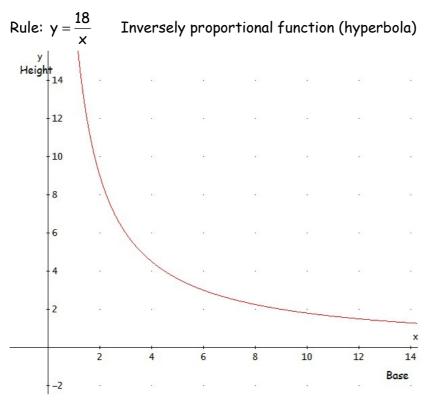
 $y = \frac{x}{2} + 1$ is a straight line, with slope 1/2 (increasing) and y-intercept (0, 1)



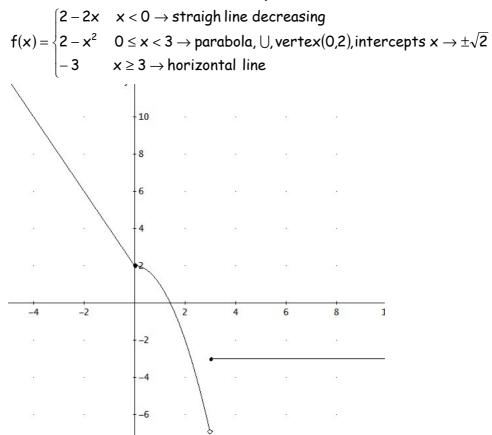
2. The labels stuck on tins of tomatoes are rectangular which an area of 18 cm². What are the possible lengths of the base and height? Make a table with some of the possibilities and graph the function. Find the rule. What type of function is it?

Base	1	2	3	6	9	18
Height	18	9	6	3	2	1





3. Sketch the graph of the compound function (to graph the function write its characteristics and don't use a table data):



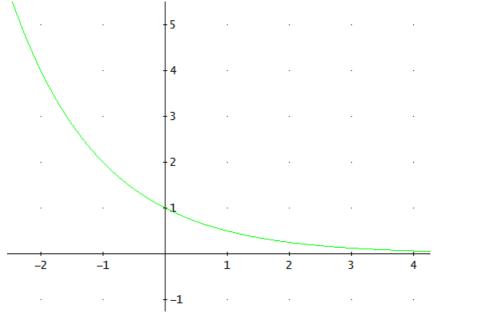


- a) Domain and range Dom = R , $R = (-7, +\infty)$
- b) Increasing and decreasing intervals: decreasing in $(-\infty,3)$, constant in $(3,+\infty)$
- c) Continuity: It is continuous in $R \{3\}$, It has a jump discontinuity in x = 3

4. In the following equations, find x:

- a) $\log_3 9^x = 2 \rightarrow 3^2 = 9^x \rightarrow 3^2 = 3^{2x} \Longrightarrow x = 1$
- b) $\log_5(x+2) = 3 \rightarrow 5^3 = x+2 \rightarrow 125 = x+2 \Rightarrow x = 123$
- c) $3^{x^2-6} = \frac{1}{27} \rightarrow 3^{x^2-6} = 3^{-3} \rightarrow x^2 6 = -3 \Longrightarrow x^2 = 9 \Longrightarrow x = \pm 3$
- d) log_x 16 = -2 \rightarrow x⁻² = 16 \rightarrow x² = $\frac{1}{16}$ \rightarrow x = $\frac{1}{4}$ (just positive)
- 5. Sketch the graph of the function $y = \left(\frac{1}{2}\right)^x$ What type of function is it? Write its characteristics.

It is an exponential function, base < 1, Domain R, Range $(0,+\infty)$ decreasing, continuous in R, horizontal asymptote x-axis (y=0)



Using the basic $y = \left(\frac{1}{2}\right)^x$, sketch the graph of $y = \left(\frac{1}{2}\right)^x - 2$ and $y = \left(\frac{1}{2}\right)^{x+3}$. Find their intersections with x-axis and y-axis, if possible, their domains, ranges and

asymptotes. $y = \left(\frac{1}{2}\right)^{x} - 2$ the same graph, two units down

